Sensitivity analysis of point and parametric pedotransfer functions for estimating water retention of soils in Algeria

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Abstract

Improving the accuracy of pedotransfer functions (PTFs) requires studying how prediction uncertainty can be apportioned to different sources of uncertainty in inputs. In this study, the question addressed was: Which variable input is the main or best complementary predictor of water retention, and at which water potential? Two approaches were adopted to generate PTFs: multiple linear regressions (MLR) for point PTFs; and multiple non-linear regressions (MNLR) for parametric PTFs. Reliability tests showed that point PTFs provided better estimates than parametric PTFs (RMSE: 0.0414; 0.0444 cm^3 cm^{-3} and 0.0613; 0.0605 cm^3 cm^{-3} at -33 kPa and -1500 kPa, respectively). The local parametric PTFs provided better estimates than Rosetta PTFs at -33 kPa. No significant difference in accuracy, however, was found between the parametric PTFs and Rosetta H2 at -1500 kPa, with RMSE values of 0.0605 cm^3 cm^{-3} and 0.0636 cm^3 cm^{-3}, respectively. The results of global sensitivity analyses (GSAs) showed that the mathematical formalism of PTFs and their input variables reacted differently in terms of point pressure and texture. The point and parametric PTFs were sensitive mainly to the sand fraction in the fine and medium textural classes. The use of clay percentage (C %) and bulk density (BD) as inputs in the medium textural class improved the estimation of PTFs at -33 kPa.

Keywords: soil-water retention, multiple regressions, pedotransfer function, sensitivity

I. Introduction

Predictive information on the spatial distribution of soil water and its availability for plants enables producers to take effective decisions (e.g., on nutrient management and plant cover) to maximize profitability. The soil-water balance is central to many processes that influence plant growth and the degradation of soil and water resources.

Hydrologists face the situation where soil hydraulic data such as water retention or hydraulic conductivity are often missing. Therefore, pedotransfer functions (PTFs) are used as an alternative to estimate these properties. The extrapolation of PTFs in different agropedoclimatic context limits their performance (Touil et al., 2016). The development of local PTFs could be useful in meeting the agricultural requirements for modelling with reasonable accuracy.

Soil-water retention (SWR) curves can usually be estimated using two approaches: point PTFs and parameter PTFs. With point PTFs, SWR is estimated at defined pressure points (Pachepsky et

al., 1996; Minasny et al., 1999). One of the most commonly used SWR curves is the Van Genuchten model (1980). With parameter PTFs, the parameters of SWR models, such as θs, θr, α and n, are estimated by fitting them to the data and then relating then by empirical correlation to basic soil properties (Vereecken et al., 1992; Wösten et al., 1995; Schaap et al., 1998; Minasny and McBratney, 2002; Rawls and Brakensiek, 1985; Van Genuchten et al., 1992; Wösten et al., 2001; Vereecken et al., 2010). Schaap et al. (2001) developed the Rosetta package based on the artificial neural network (ANN) method, which uses five hierarchical models to predict the van Genuchten (VG) parameters (θs, θr, α and n) with soil texture classes only and the input data (texture, bulk density [BD], and one or two water content values at -33 and -1500 kPa).

PTFs for point and parametric estimation of SWR from basic soil properties can be developed using multiple regression methods (Lin et al., 1999; Mayr and Jarvis, 1999; Tomasella et al., 2000). Some 97% of water retention PTFs for soils in the tropics are based on multiple linear and polynomial regressions of nth order techniques (Botula et al. 2014).

Using PTFs in environments that differ from those from which they were derived can lead to an under- or overestimation of SWR. Several studies have shown that SWR is a complex function of soil structure and composition (Rawls et al., 1991; Wösten et al., 2001; Rawls et al., 2003; Mirus et al., 2015). Applying PTFs to different textural or structural classes could also be a source of uncertainty (Bruand et al., 2002; Pachepsky et al., 2003). SWR and hydraulic conductivity vary widely and non-linearly with soil-water potential. Soil texture is the main determinant of the water-holding characteristics of most agricultural soils (Saxton et al., 1986). The relationship between the SWR curve and particle size distribution (PSD) has been investigated in many studies (Jonasson et al., 1992; Minasny et al., 2006; Ghanbarian et al., 2009; Xu Yang et al., 2013; Tae-Kyu Lee et al., 2014). SWR depends mainly on texture, with other factors such as BD, structure, organic matter (OM), clay type and hysteresis having a secondary impact (Williams et al., 1983, Saxton et al., 1986, Vereecken et al., 1989, Winfield et al., 2006).

The variability in PTF response depends on the variability and uncertainty of one or more of the input variables. Uncertainty analysis in the variety of available PTF approaches is necessary to minimize error in estimation and identify its source. Recently, sensitivity analysis techniques and uncertainty analysis have begun to receive considerable attention in PTF studies (Nemes et al., 2006b; Kay et al., 1997; Grunwald et al., 2001; Deng et al., 2009; Moeys et al., 2012; Loosvelt et al., 2013). The question is: Which variable input is the main or best complementary predictor of SWR, and at which potential? Global sensitivity analysis (GSA) enables us to study how uncertainty in the output of a model can be apportioned to different sources of uncertainty in the model inputs (Saltelli et al., 2000). Generally, GSA is useful for identifying which variables make the main contribution to output variables (Jaques et al., 2004).

The objectives of this study were to:
- Develop and validate two PTF approaches using regression methods: point PTFs for estimating SWR in Algerian soils at -33 kPa and -1500 kPa; and parametric PTFs for estimating the VG parameters

83 • Study the impact of each input on the PTF responses

II. Materials and methods

1. The database

The soil dataset used for this study was collected from various regions in Algeria, mainly in the north, which has a Mediterranean climate. It contained 242 samples, with basic soil properties: texture fractions (based on the USDA system; clay and silty-clayey for most of the soils, Fig. 1a), Bulk density (BD), organic matter percentage (OM) and water content at -33 kPa and -1500kPa. Descriptive statistics of the development and validation datasets are presented in Table 1. The available database was split into two datasets. Subset 1, which was used to develop the PTFs, contained 78.1% of the samples. Used as the calibration set, they were collected from the coastal plain of Annaba in north-eastern Algeria (13 samples), the Beni Slimane plain of Media (42 samples), the Kherba El Abadia plain of Ain Defla (54 samples) and the Lower Cheliff plain in north-western Algeria (80 samples). Subset 2 contained the remaining 21.9% of the samples. Used to verify the PTFs, they were collected from Benziane valley in the lower south-western Cheliff plain. The depth of the two upper horizons varied from site to site, with a maximum of 30 cm for surface horizons and more than 30 cm for subsurface horizons.

Particle size distribution (PSD) analysis was conducted using the international Robinson's pipette method (Robinson, 1922). Undisturbed soil samples obtained with 500-1,000 cm^3 cylinders were used to determine BD. The SWR values at -33 kPa and -1500 kPa were obtained using Richards's apparatus (Richards et al., 1943). Undisturbed soil samples were collected near field capacity with 100 cm^3 cylinders. Water content was measured using the gravimetric method at 105°C (24 h). Organic carbon content was determined using the wet oxidation method (Walkley and Black, 1934). Variation in soil texture in the dataset is displayed using the textural triangle proposed by FAO (1990) in Figure 1b.

The SWR model devised by Van Genuchten (1980) is defined as:

$$\theta(h) = \theta_r + \frac{\theta_s - \theta_r}{(1 + |\alpha h|^n)^m} \tag{1}$$

Where θ_r and θ_s are residual and saturated soil-water content (cm^3 cm^{-3}), respectively, and α (cm^{-1}) and n are the shape factors of the SWR function. The VG parameters were indirectly estimated for each soil sample from four levels of measured data inputs: sand, silt and clay percentages, and BD using the Rosetta model H3 (Schaap et al., 2001). The 'm' parameter was calculated as follows:

m = 1 -1 / n.

2. PTF development

Two approaches were used in this study to develop the PTFs: point PTFs for estimating SWR for particular points of pressure (h); and parametric PTFs for predicting the VG parameters. Each water content level at selected water potentials of -33 kPa and -1500 kPa and estimated VG

parameters were related to basic soil properties (i.e., sand, silt, clay content, OM content and BD) using multiple regression techniques (Table 2). The most significant input variables were determined using the Pearson correlation (α =5%). For the multiple-linear regression (MLR) models, the general form of the resulting equations was expressed thus:

$$Y= a_0+ b_1 X_1 + b_2 X_2 + b_3 X_3 + b_4 X_4 \tag{2}$$

For the multiple-non-linear regression (MNLR) models, it was expressed thus:

$$Y= a_0 + b_1 X_1 + b_2 X_2 + b_3 X_1{}^2 + b_4 X_2{}^2 + b_5 X_1{}^3 + b_6 X_2{}^3 + b_7 X_1{}^* X_2 + b_8 X_1{}^2{}^* X_2 + b_9 X_1{}^* X_2{}^2 \tag{3}$$

Where Y represents the dependent variable, a_0 is the intercept; b_1…, b_n are the regression coefficients, and X_1 to X_4 refer to the independent variables representing the basic soil properties.

The prediction quality of the point and parametric PTFs developed from Algerian soils were then compared with three Rosetta PTFs (H1, H2 and H3). We chose the Rosetta model because it gives the user flexibility in inputting the data required (Stumpp et al., 2009), with the option of five levels based on input data (Schaap et al. 2002):

- H1: Textural classes (USDA system)
- H2 : Clay+Silt+Sand
- H3: Clay+Silt+Sand+ BD
- H4: Clay+Silt+Sand+ BD +Volumetric water at -33 kPa
- H5: Clay+Silt+Sand+ BD +Volumetric water at -33 kPa + Volumetric water at -1500 kPa

The Rosetta model was also chosen because it has given reasonable predictions in several evaluation studies (Frederick et al., 2004, Nemes et al., 2003). In our study, the three Rosetta model levels (H1, H2, and H3) were selected to compare their performance in the Algerian soils because they require only texture data and BD as inputs, as locally developed PTFs do.

3. Evaluation criteria

PTFs are regularly assessed by comparing the values that they predict with the measured values (Pachepsky and Rawls, 1999). In order to assess the validity of the PTFs developed, we used the following criteria: mean prediction error (ME) to indicate the bias of the estimate; root mean square error (RMSE) to assess the quality of the prediction (it is frequently used in studies on PTFs); and the index of agreement (d) developed by Willmott and Wicks (1980) and Willmott (1981) as a standardized measure of the degree of model prediction error. They were calculated using the following equations, respectively:

$$\boldsymbol{ME} = \frac{1}{N} \sum_{i=1}^{n} (\theta_p - \theta_m) \tag{4}$$

Where N is number of horizons, and θ_p, θ_m, predicted and measured volumetric water content, respectively. The estimate was better when ME was close to 0'. Negative ME values indicated an average underestimation of θm, whereas positive values indicated overestimation.

161 $$RMSE = \left\{\frac{1}{n}\sum_{i=1}^{n}(\theta_{\mathrm{p}}-\theta_{\mathrm{m}})^2\right\}^{\frac{1}{2}}$$ (5)

162 Thus, the lower the RMSE, the better the estimate.

163 $$d = 1 - \frac{\sum_{i=1}^{n}(\theta_{\mathrm{p}}-\theta_{\mathrm{m}})^2}{\sum_{i=1}^{n}[|(\theta_{\mathrm{p}}-\bar{\theta}_{\mathrm{m}})|+|(\theta_{\mathrm{m}}-\bar{\theta}_{\mathrm{m}})|]^2}$$ (6)

164
165 The index of agreement varied from 0 to 1, with higher index values indicating that the modeled values
166 θ_{p} were in better agreement with the observations θ_{m}.

167

168   4.   Global sensitivity analysis (GSA)

169

170 GSA involves determining which part of the variance in model response is due to variance in which
171 input variable or group of inputs. The impact of the parameters is quantified by calculating the global
172 sensitivity indices.
173   The Sobol method (Sobol, 1990) is an independent GSA method based on decomposition of
174 the variance. When the model is non-linear and non-monotonic, the decomposition of the output
175 variance is still defined and can be used. The Sobol model is represented by the following function:
176

177   *Y= f (X₁, X₂, X₃,........,Xₚ)* (7)

178 Where Y is the model output (or objective function) and $X=(X_1,....., X_p)$ is the input variable set.

179   V(Y) = V (E (Y|X)) + E (Var (Y|X)) (8)

180

181 Where V(Y) is the total variance in the model, V (E(Y|X)) and E (Var(Y|X)) signify variance in the
182 conditional expected value and expected value of the conditional variance, respectively. When the
183 input variables X_i are independent, the variance decomposition of the model is:

184 $$V(Y) = \sum_{i=1}^{p}V_i + \sum_i\sum_j V_{ij} + + \sum_i\sum_j\sum_p V_{ijp} + \ldots\ldots + V_{1,2,3,\ldots p}$$ (9)

185   *Vᵢ = V [E(Y|Xᵢ)]*
186   *Vᵢⱼ = V [E(Y|Xᵢ, Xⱼ)] -Vᵢ-Vⱼ*
187   *Vᵢⱼₚ= V [E(Y|Xᵢ, Xⱼ, Xₚ)] - Vᵢⱼ - Vᵢₚ - Vⱼₚ - Vᵢ - Vⱼ - Vₚ*

188
189 Where V_i is the proportion of variance due to variable X_i. Dividing V_i by V(Y) produces the expression
190 of the first-order sensitivity index (S_i), such that:

191

192 $$S_i = \frac{V_i}{V(Y)} = \frac{V[E(Y/X_i)]}{V(Y)}$$ (10)

193 The term S_i is the measure that guarantees an informed choice in cases where the factors are
194 correlated and interact (Saltelli and Tarantola, 2002). This index is always between 0 and 1, and
195 represents a proper measurement of the sensitivity used to classify the input variables in order of
196 importance (Saltelli and Tarantola, 2001).

197 In order to quantify variation in the sensitivity index (V_{Si}) of an input factor X_i, we fixed it at $Xi = Xi *$

198 ($Xi *$: the average when the variable follows the normal distribution, the median when the variable

199 follows the lognormal distribution). In order to calculate how much this assumption changed the

200 variance of Y, we used this formula:

201 $V_{Si} = \left(\frac{V[E(Y/X)]}{V(Y)} - \frac{V[E(Y/Xi=Xi*)]}{V(Y)} \right) * 100$ (11)

202 $V_{Si} > 0$ and S_i close to 1 indicate increasing accuracy of PTFs;

203 $V_{Si} < 0$ and S_i close to 1 indicate increasing accuracy of PTFs;

204 $V_{Si} > 0$ and S_i close to 0 indicate decreasing accuracy of PTFs;

205 $V_{Si} < 0$ and S_i close to 0 indicate decreasing accuracy of PTFs.

206 In addition, combining the RMSE and S_i enabled us to detect the contribution of each variable to

207 improvement in the quality of prediction of the PTFs.

208

209 **III.   Results and discussion**

210

211 In Table 3, most of the PTFs underestimated SWR except for the point PTF at the two

212 pressure points (-33 kPa and -1500 kPa). The Rosetta H2 model, which considers only texture as an

213 input, gave a ME values close to zero than the H1 and H3 models (- 0.0728; -0.0436 $cm^3 cm^{-3}$ at -33

214 kPa and -1500 kPa, respectively).

215 The poor ME values indicated better estimates of PTFs. They were produced after the

216 application of point PTFs followed by parametric PTFs (Figure 2).

217 Among the five tested models in the Lower Cheliff soils, the point PTFs (MLR) derived from a

218 database taken from some Algerian soils had the lowest RMSE values (0.041 and 0.044 $cm^3 cm^{-3}$ at -

219 33 kPa and -1500 kPa, respectively). Performances equivalent or superior to PTFs derived by multiple

220 regression methods have been reported in some studies (Minasny et al., 1999; Nemes et al., 2003).

221 The non-linear models (parametric PTFs), however, gave a better estimation than the Rosetta models

222 based on ANN (RMSE: 0.0613 and 0.0605 $cm^3 cm^{-3}$ at -33 kPa and -1500 kPa, respectively). The

223 RMSE and ME values of the three Rosetta models also showed that H2 was better than H1 or H3

224 (Table 3, Figure 3).

225 The index of agreement results showed that point PTFs were more suitable for Lower Cheliff

226 soils than parametric PTFs (Table 3 3), with values of 0.9975 and 0.9911 $cm^3 cm^{-3}$). Similar

227 comparisons in different regions were undertaken by Minasny et al. (1999), Tomasella et al. (2003)

228 and Ghorbani Dashtaki et al. (2010), who all reported similar differences between these two PTF

229 approaches. As Table 3 shows, there was no significant difference in RMSE values between the

230 parametric PTFs and Rosetta H2 at -1500 kPa (RMSE: 0.0605 $cm^3 cm^{-3}$ and 0.0636 $cm^3 cm^{-3}$,

231 respectively).

232
233   1.   Sensitivity index before textural grouping
234

235   In the development of PTFs, using PSD as an input is the usual approach (texture as an
236 overall expression of PSD, clay, silt and sand content) and its contribution is fundamental to
237 understanding the process of retaining water at different pressure points, although various physical
238 and chemical characteristics are used to describe the SWR curve, such as BD and OM.
239   The importance of each input variable was assessed by the first order S_i. It was clear for the
240 PTFs developed that OM% and clay percentages (C %) were the variables with the greatest impact
241 (Figure 4). For the point PTFs (MLR), the most sensitive estimations were at two pressure points (S_i:
242 0.821; 0.782 at -33 kPa and 0.630; 0.585 at -1500 kPa for OM% and C%, respectively). The
243 percentage of silt (S_i %) was second in importance in parametric PTFs (0.576 at -33 kPa) after OM,
244 followed by BD and C (Fig. 2). The S_i values placed sand content in third place in the MLR
245 (0.262; 0.162), indicating that its impact on the parametric model was almost insignificant, with very
246 low values (S_i: 0.077; 0.017) at -33 kPa and -1500 kPa, respectively).
247   The prediction quality of point PTFs (MLR) can be explained, first, by taking into account the
248 basic characteristics of soil as an input from the textural and structural information given by the BD.
249 Second, point PTFs (MLR) are based mainly on these input variables, unlike parameter PTFs
250 (MNLR), which have inputs other than texture and BD, as well as other parameters (VG parameters:
251 θ_r, θ_s, α, n).
252
253   2. Sensitivity and uncertainty analysis after the textural grouping
254
255   The sensitivity of the multiple regression methods (linear and non-linear) used to develop PTFs
256 from basic soil characteristics for estimating SWR for different textural classes was analyzed. We
257 grouped the samples into three classes of particles (Figure 1.b) in line with FAO guidelines (FAO,
258 1990): very fine (12 samples); fine (31 samples); and medium (10 samples).

259   The results showed that after the textural grouping, there was an improvement in the quality
260 estimation of PTFs only in the medium class. A better prediction at -1500 kPa was provided by point
261 PTFs (RMSE = 0.027 cm^3 cm^{-3}) and parametric PTFs (RMSE = 0.038 cm^3 cm^{-3}) at -1500 kPa (Figure
262 5).
263 **1. Texture:** After textural grouping, the MLR and MNLR PTFs developed were always sensitive
264 mainly to the sand fraction in the fine and medium classes (Table 4). The variation in the first S_i in
265 the point PTFs was significantly greater in the medium texture class at the two pressure points (-33
266 kPa and -1500 kPa). In the MNLR, sand had the most influence, particularly with regard to the fine
267 class (-40.9%, 18.9% at -33 kPa and 1500 kPa) and the medium class (-16.7% at -1500 kPa).
268 The S_i of a variable quantifies the influence of its uncertainty on the output. This is the part of the
269 variability output explained by the variability input. What was confirmed after calculating the variation
270 in the first order S_i was that the PTFs developed were still more influenced by the variability in sand at
271 -33 kPa than at -1500 kPa. This impact could be explained by the irregularity of the dispersion of sand
272 content in the validation database, with a coefficient of variation (CV) of about 119% compared with
273 the other input variables (33%, 18%, 9% and 57% for clay, silt, BD and OM, respectively). This
274 heterogeneity in the sand data series clearly influenced the uncertainty of the PTF response.

275 Looking at the matrix correlation (Table 5), the clay and silt fractions were significantly correlated with
276 sand content. Saltelli and Tarantola (2002) observed that when X_1 and X_2 were correlated with a third
277 factor, X_3, the S_i calculated depended on the force of this correlation as well as the distribution of X_3. In
278 this case, the index power could be influenced by this statistical association, as it explains the higher
279 value difference of index variation in the sand percentage compared with the other variables.

280 We observed that point PTF (MLR) produced a lower error of estimation when the variation of the first
281 order S_i for sand was the most important (MLR in the medium class: RMSE 0.030 cm^3 cm^{-3}; 0.027 cm^3
282 cm^{-3} with V_{Si} -103% and 86.4% at -33 kPa and -1500 kPa, respectively). A negative S_i variation in
283 sand content when the latter was fixed was apparent in all texture classes (Table 4). This could be
284 explained by the proportional relationship between sand and clay content, particularly in the validation
285 dataset with a dominant clay texture. Insignificant sensitivity of sand was recorded for the very fine
286 texture. Rawls et al. (2003) observed that 10% of sand provides an increase in SWR at low clay
287 content and a decrease in SWR at high clay content of more than 50%.

288 The relationship between VG's SWR curve parameters (especially n and α) and PSD has been
289 examined in many studies (e.g., Minasny et al., 2007; Benson et al., 2014) in order to explain why the
290 sand impact increases in the fine texture class in parametric PTFs. It could be explained by the
291 predominant presence of sand and clay content as inputs in parametric PTFs. For soils with clay
292 content between 35% and 70%, water content is greatly influenced by the percentage of sand in the
293 soil (Loosvelt et al., 2013).

294 In addition, when the sand content of a sample increased to 60%, the drying rate was faster and water
295 absorbing ability was weaker than with the low sand content. When sand content falls to 20%, the
296 small pores occupy a large part of the pore structure, making the soil compact (Hao et al., 2015).
297 In the medium texture class, there was increasing accuracy in PTFs at -33 kPa after fixing the clay
298 content. This could be explained by the reduced clay percentage in the medium class (mean of clay
299 (%) = 23%), which produced fewer errors at -33 kPa.
300 The accuracy of the PTFs decreased when they were applied to some soil samples with a clay content
301 > 60% (Figure 5). In the very fine class, insignificant sensitivity was recorded at all pressures defined
302 in this study. In this class, the variation in clay was much lower because it is only the dominant solid
303 fraction, which could explain the smaller variation in S_i after fixing the clay percentage.. The greatest
304 impact of clay (%) was observed at -1500 kPa in the point and parametric PTFs in different textural
305 classes (Figure 6). The clay content of soils is a major predictor for modelling the permanent wilting
306 point of soils (Minasny et al., 1999).
307 The silt percentage was introduced as an explanatory variable only in parametric PTFs (MNLR). This
308 fraction is known for its ability to retain water at high and medium soil water potentials. The GSA
309 showed that the silt percentage had a stronger impact on the estimation of parametric PTFs at -1500
310 kPa than at -33 kPa with the MNLR model. After textural grouping, an important variation in the first
311 order S_i was observed in the medium class (-36.7% to -1500 kPa). The lowest values were recorded
312 in the very fine class. It was clear that the silt percentage has an important role in estimating VG's
313 parameters (α, n), and that its use as an input influences the estimate in the medium and fine classes.

There was an increasing accuracy, however, in the PTFs recorded in the fine class at -1500 kPa. With silt and clay as inputs, there was a better estimation. Plant-available water content variation is more related to sand and silt than to clay content (Reichert et al., 2009).

2. Bulk density: this is the second most influential variable on the point PTF (MLR) response on all textural class. The important variation of sensitivity index is noted mainly in the very fine textural class at -33 kPa (V_{Si} = -50, 5%). In parametric PTFs, BD influenced the medium class at -33 kPa. The accuracy of quality estimation at - 33 kPa in the medium class when fixing the BD for the two PTF approaches (Table 4). The very fine textural class represented 16 surface samples (0–30 cm) with a dominance of clay texture. In a similar study on clay soils, volumetric water content (VWC) was highly related to the inverse of BD at field capacity (Bruand et al., 1996). The inclusion of BD as an input provides information on pore volume, which can influence the performance of PTFs when applied to soil with high clay content. In addition, the soil structural information characterized by BD measurements is an indirect measurement of pore space and is affected mainly by texture and structure. For structureless soils, primarily coarse and medium textured soils, the pore-size distribution can be satisfactorily described by PSD. The medium texture is related in general to pore-size distribution, as large particles give rise to large pores between them, and therefore have a major influence on the SWR curve (Arya and Paris, 1981; Nimmo, 2004). With BD and texture as inputs in point PTF (MLR), predicted values very close to the experimental results are obtained.

3. Organic matter content: The less insignificant variation in the S_i after textural grouping is related to OM content. This could be explained, first, by the poor OM content in the Algerian soil samples. Lal (1979) did not find any effect of OM content on SWR. Danalatos et al. (1994) attributed this to the generally low OM content in their samples. Second, homogeneity of the data for OM content in every textural class reduced the variation in PTF response. The increasing accuracy of parametric PTFs, however, was apparent for medium-textured soils at -33 kPa, where OM was used as an input to predict θ_s. SWR at -33 kPa is affected more strongly by organic carbon than at -1500 kPa (Rawls et al., 2003). The sensitivity analysis conducted by Rawls et al. (2003) to study the role of OM content as a predictor showed that the SWR of coarse-textured soils is much more sensitive to changes in organic carbon than is the case with fine-textured soils. Bauer and Black (1981) found that the effect of organic carbon on SWR in disturbed samples was substantial in sandy soil and marginal in medium and fine textured soils.

IV. Conclusion

The objective of this study was to analyze the sensitivity of estimating the SWR properties of Algerian soils using PTFs. We developed and validated point and parametric PTFs from basic soil properties using regression techniques and compared their predictive capabilities with the Rosetta models (H1, H2, and H3). The reliability tests showed that point PTFs produce more accurate estimations than parametric PTFs. The derived parametric PTFs, however, provided better estimates than the Rosetta models originally developed from a large intercontinental database.

The GSA showed that the mathematical formalism of the PTF models and their input variables reacted differently in terms of point pressure and textural class:

- After textural grouping, the two PTF approaches developed (MLR and MNLR) were always sensitive primarily to the sand fraction in the fine and medium classes at -33 kPa, rather than at -1500 kPa.
- The results illustrated the accuracy of estimation at -33 kPa in the medium class for the two PTF approaches when fixing the clay percentage (C %) and BD.
- The accuracy of PTFs decreased when they were applied to soil samples with a clay content > 60%.
- The most insignificant variation in the S_i after textural grouping was related to the OM content in Algerian soils.

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538 **Tables:**

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541 **Table 1**. Soil characteristics of the developed and validated datasets.

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	PSD					VWC (cm^3 cm^{-3})	
	S (%)	Si (%)	C (%)	BD (g/cm^3)	OM (%)	- 33 kPa	-1500 kPa
Samples used for deriving PTF (n = 189)							
Average	17.81	39,23	42.97	1.71	0.95	0.44	0.27
Standard deviation	10.32	10.76	13.90	0.20	0. 93	0.09	0.08
Min	1.00	9.20	4.00	0.60	0.08	0.13	0.03
Max	50.00	67.00	84.30	2.10	8.40	0.73	0.56
Coefficient of variation (CV)	0.58	0.27	0.32	0.12	0.98	0.21	0.31
Samples used for testing PTF (n = 53)							
Average	12.50	41.58	45.92	1.49	0.87	0.40	0.21
Standard deviation	14.84	7.62	14.94	0.13	0.50	0.10	0.07
Min	-	29.00	9.00	1.15	0.20	0.14	0.07
Max	59.00	58.00	70.00	1.73	2.74	0.57	0.45
Coefficient of variation (CV)	1.19	0.18	0.33	0.09	0.57	0.24	0.35

543 *(*) S: sand, C: clay, Si: silt, BD: bulk density, OM: organic matter, PSD: particle size distribution, VWC: volumetric*
544 *water content*

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546 **Table 2**. Developed pedotransfer functions

Point PTFs

   at -33 kPa: *θ = 0.0246 − 0.0040*S + 0.0012*C + 0.2554*BD + 0.0067 * OM*

   at -1500 kPa: *θ = - 0.0627 − 0.0029*S + 0.00165*C + 0.1837*BD + 0,0017* OM*

Parametric PTFs

θ s *= 0,44 - 0,0013369*S + 0,0002*C + 0,01771343* BD - 0,0018272* OM*

θ r *= 0,09 + 0,000777943*S - 0,000319883* C + 0,000063602*S^2 + 0,000012*C^2 + 0,00000093*S^3 - 0,0000001* C^3*

α *= 0,003 - 0,0001*S + 0,000089* Si + 0,0000054*S^2 - 0,0000045*Si^2 - 0,000000073*S^3 + 0,000000045*Si^3 + 0,0000077*S*Si - 0,000000031* S^2 *Si - 0,000000062*S*Si^2*

n *= 2,9 - 0,00277395*C - 0,09478943* Si - 0,00036644 * C^2 + 0,00202592*Si^2 + 0,00000249*C^3 - 0,000015*Si^3 + 0,00028374* C*Si + 0,00000491* C^2 * Si - 0,00000532*C*Si^2*

547 *S: sand (%), C: clay (%), Si: silt (%), BD: bulk density (g/cm^3), OM: organic matter (%), θr and θs are residual and*
548 *saturated soil-water content (cm3 cm–3), respectively, and α (cm–1) and n are the shape factors of the of van*
549 *Genuchten model.*

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563 **Table 3.** Evaluation criteria of water retention pedotransfer functions (PTFs) at -33 kPa and -1500 kPa.
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			-33 kPa	*-1500 kPa*
ME (cm³ cm⁻³)	*Point PTF*	MLR	0.0188	0.0261
	Parametric PTF	MNLR	-0,0016	-0.0020
	Rosetta	H1	- 0.0902	-0.0458
		H2	- 0.0728	-0.0436
		H3	-0.0991	-0.0552
RMSE (cm³ cm⁻³)	*Point PTF*	MLR	0.0414	0.0444
	Parametric PTF	MNLR	0.0613	0.0605
	Rosetta	H1	0.1170	0.0738
		H2	0.0970	0.0636
		H3	0.1280	0.0749
d (cm³ cm⁻³)	*Point PTF*	MLR	0.9975	0.9911
	Parametric PTF	MNLR	0.9938	0.9775
	Rosetta	H1	0.9623	0.9427
		H2	0.9775	0.9597
		H3	0.9519	0.9331

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567 **Table 4.** Variation of first order sensitivity index (S_i) in the different textural classes.

		Tex-class	Si (%) V_{Si}	A.E	S (%) V_{Si}	A.E	C (%) V_{Si}	A.E	BD (g/cm³) V_{Si}	A.E	OM (%) V_{Si}	A.E
RML	**at -33 kPa**	**VF**	*Abs*		-1.2		-0.4		-50.5	-	4.6	
		F	*Abs*		-43.2	-	-10.7	-	-39.9	-	0.2	
		M	*Abs*		-103.3	-	-27.5	+	-44.4	+	-5.7	
	at -1500 kPa	**VF**	*Abs*		-0.3		0.9		-27.3	-	1.1	
		F	*Abs*		-46.2	-	-20.7	-	-41.6	-	0.1	
		M	*Abs*		-86.4	-	-52.9	-	-22.9	-	-2.3	
MNLR	**at -33 kPa**	**VF**	0.4		-0.2		0.1		-00.1		-0.05	
		F	-1.6		-40.9	-	-1.1		-2.5		-0.1	
		M	15.0		-5.2		15.1	+	21.6	+	22.3	+
	at -1500 kPa	**VF**	- 4.6		-0.3		-1.8		-1.4		-00.5	
		F	28.6	+	18.9	-	4.6		0.4		0.1	
		M	-36.7	-	-16.7	-	-22.6	-	8.9		-8.4	

568 *Abs: absent in the model, V Si: variation first sensitivity index;   A.E.: improving estimation.*

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570 **Table 5.** Pearson correlation matrix between basic soil characteristics in the validation dataset of 53
571 soil samples.

Variables	S_i (%)	C (%)	S (%)	BD (g/cm³)	OM (%)
Si%	**1**				
S %	**-0.334**	**1**			
C %	-0.159	**-0.878**	**1**		
BD (g/cm3)	0.164	-0.185	0.11	**1**	
OM (g/100g)	-0.174	-0.166	0.263	-0.19	**1**

The values in bold differ from 0 to a level of significance α = 0.05
Si: silt, S: sand, C: clay, BD: bulk density, OM: organic matter

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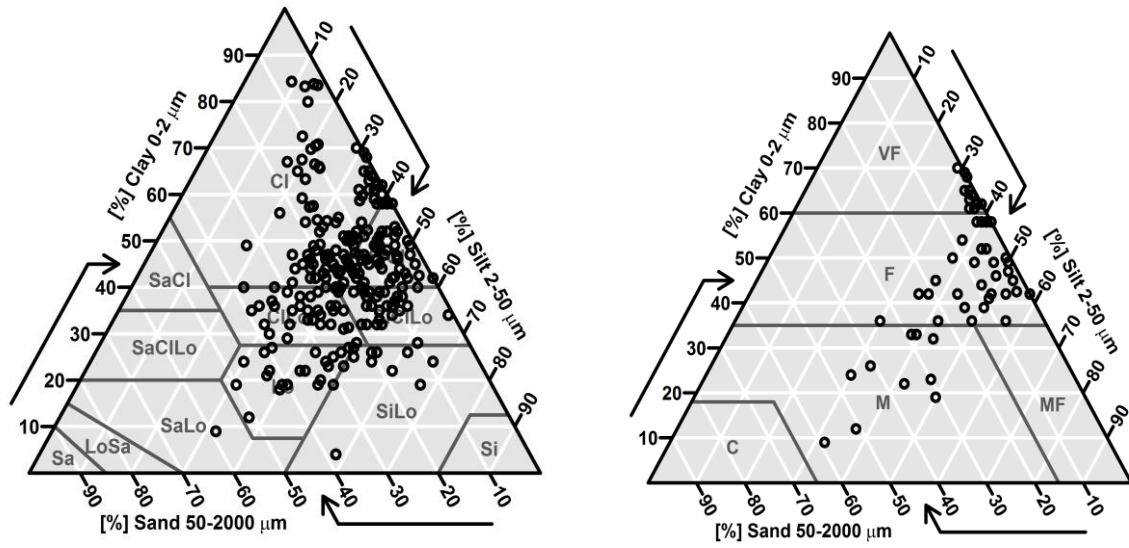
595 **Figure 1**. (a): Texture fractions of dataset (242 samples) based on USDA system. (b): Particle size
596 distribution of 53 soil samples from Algeria according to FAO textural triangle (FAO, 1990).
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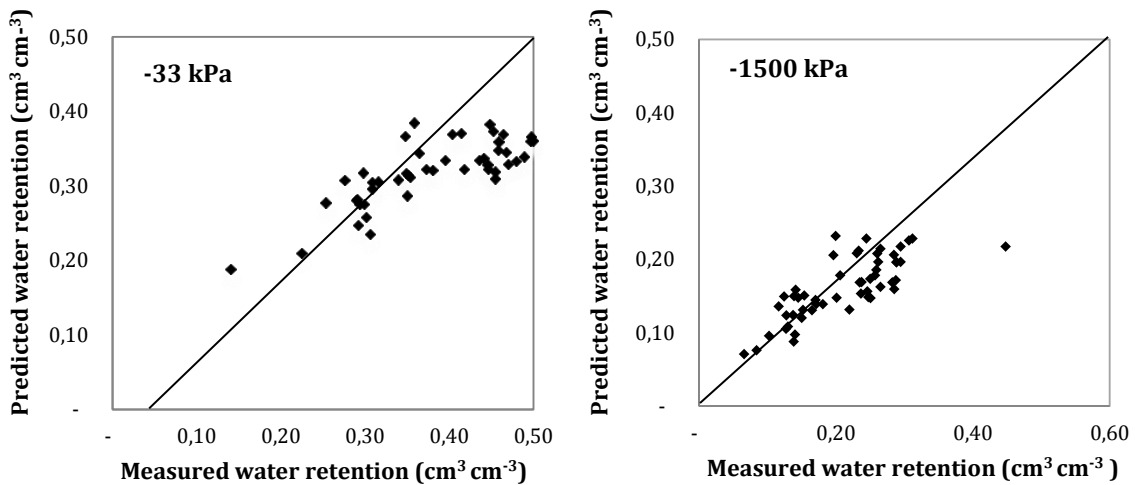
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599 **Figure 2**. Scatter plots of measured versus predicted soil water retention by Rosetta H2.
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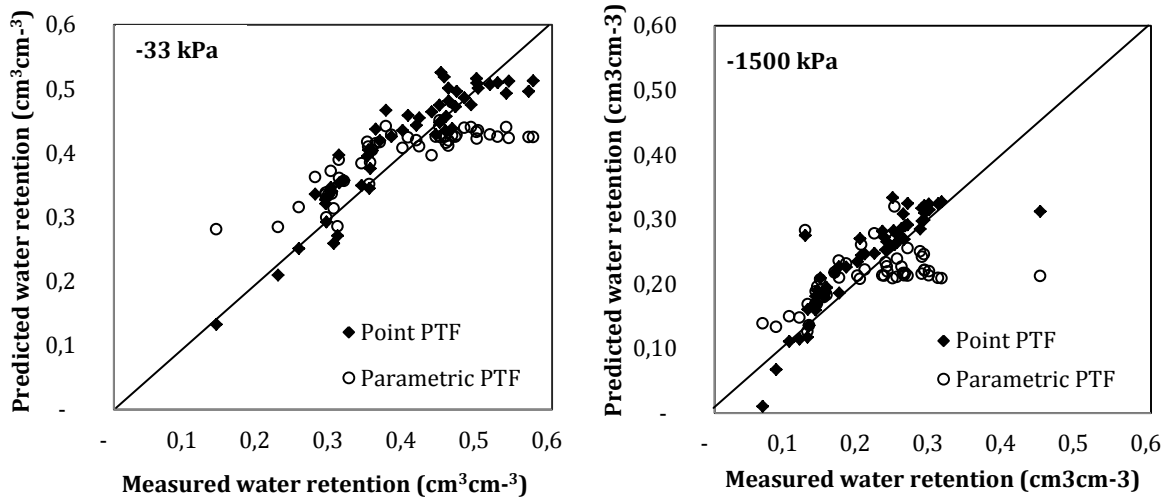
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602 **Figure 3.** Scatter plots of measured soil water retention versus predicted soil water retention.
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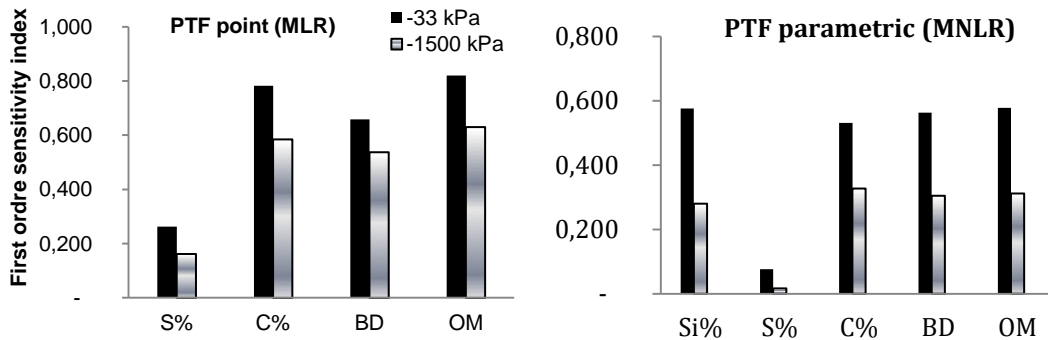
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605 **Figure 4.** First order sensitivity index.
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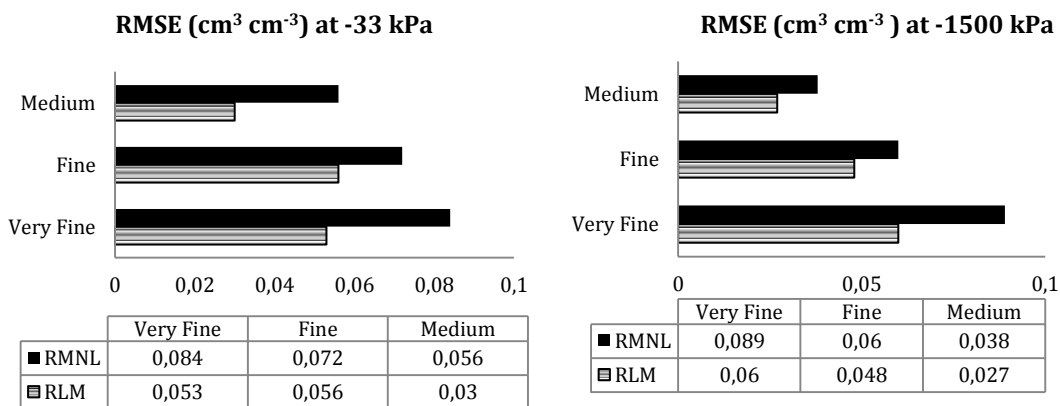
	Very Fine	Fine	Medium
■ RMNL	0,084	0,072	0,056
▤ RLM	0,053	0,056	0,03

	Very Fine	Fine	Medium
■ RMNL	0,089	0,06	0,038
▤ RLM	0,06	0,048	0,027

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610 **Figure 5.** Root mean square error (RMSE) values calculated for the different textural classes.

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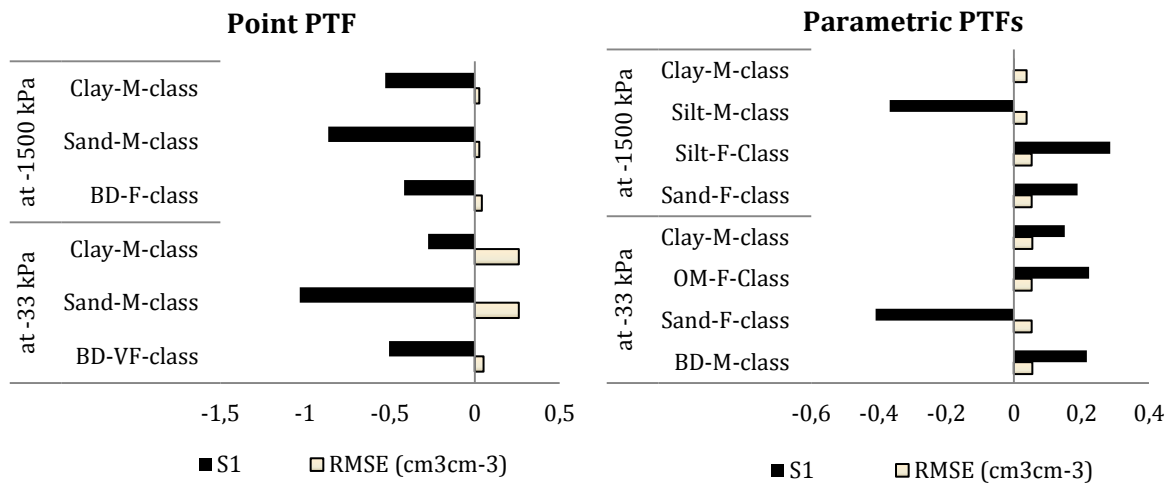
Figure 6. Variation in first sensitivity index with RMSE after textural grouping.