

1 Gully geometry: what are we measuring?

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7 Abstract

8 Many of the research works on (ephemeral) gully erosion comprise the determination of
9 the geometry of these eroded channels especially their width and depth. This is not a
10 simple task due to uncertainty generated by the wide range of variability of gully cross-
11 section shapes found in the field. However, in the literature, this uncertainty is not
12 recognized so that no criteria in their measurement procedures are indicated. The aim of
13 this work is to make researchers aware of the ambiguity that arises when characterizing
14 the geometry of an ephemeral gully and similar eroded channels. In addition, a
15 measurement protocol is proposed with the ultimate goal of pooling criteria in future
16 works. It is suggested the geometry of a gully could be characterized through its mean
17 equivalent width and mean equivalent depth, which, together with its length, define an
18 “equivalent prismatic gully” (EPG). The latter would facilitate the comparison between
19 each other of different gullies.

20

21 1. Introduction

22 The classic forms of water erosion are caused by non-concentrated or laminar flow and
23 concentrated flow; in the latter, rill and gully erosion has been recognized (Hutchinson
24 and Pritchard, 1976). Rill erosion is produced in the form of numerous channels of a
25 few centimeters in depth, distributed uniformly and randomly over sloping lands (Soil
26 Science Society of America, 2015), and which can easily be obliterated by conventional
27 tillage (Hutchinson and Pritchard, 1976). Also, permanent gullies are distinguished from
28 ephemeral ones (Foster, 1986; Thorne et al., 1986; Casali et al., 1999). Permanent
29 gullies are erosion channels which are too large to be eliminated by conventional tillage
30 (Soil Science Society of America, 2015). Ephemeral gullies –present in agricultural
31 soils– are, like rills, small enough for it to be possible to eliminate them by traditional
32 tillage (Soil Science Society of America, 2015), hence their being qualified as
33 ephemeral. However, when they form again, and contrary to what is observed in rills,
34 they tend to appear in the same places. This is explained by the fact that the ephemeral
35 gullies are formed in the thalweg which configures the confluence of two opposing
36 slopes, a fact which conditions the trajectory of the runoff. Rills, however, occur
37 entirely on one single slope (Casali et al., 1999); their formation is, therefore, mainly
38 subjected to the high spatial variability of intrinsic factors of the soil (structural
39 stability, hydraulic conductivity, etc.) and of its tillage.

41 The objectives of a large number of works on gully erosion have been the estimation of
42 the spatial and/or temporal evolution of a gully or a network of them under different
43 conditions (i.e. climate, land use, etc.) (e.g., Casalí et al, 2006; Gabet and Bookter,
44 2008; Campo-Bescós et al., 2013). For that purpose, as a first step, a morphological
45 characterization is made of these channels. The most frequent way to do so is by the
46 measurement of their width and depth –and the ratio between both parameters– (e.g.,
47 Giménez et al., 2009); and their typology is also studied (for example, whether their
48 cross section presents a general shape like a U or a V). If the measurement of the length
49 of the gully is added to this, it might be possible to arrive at determining their volume
50 (eroded soil).

51 Consequently, for a precise description of the geometry of a gully, the correct
52 determination of its width is a key factor. This is not always an easy task, especially
53 when faced with cross sections with intricate shapes and diffuse limits. However, in the
54 numerous scientific works on the subject, no uncertainty whatever is expressed on this
55 measurement, and neither are the criteria followed in the procedure specified. We
56 believe that, as a general rule, it is usually assumed that their width is defined by the
57 imaginary line whose ends are located at both points of the two banks, where an abrupt
58 change in slope is manifested. This criterion would be followed both in direct
59 measurements in situ, and in indirect ones taken from digital elevation models and
60 mathematic algorithms ad hoc (e.g., Evans and Lindsay, 2010; Parker et al., 2012;
61 Castillo et al., 2014). This procedure, at first sight reasonable and unquestionable,
62 raises, however, two objections. First, there is the presence of more than one point of
63 slope inflection in one or both banks. Second, although only one visible inflection point
64 is presented on the slope of each bank – with the width of the channel thus being clearly
65 defined – this poses a question. Do the limits of this channel, defined in this way, really
66 correspond to the transversal limits of the erosive process which gave rise to the gully?
67 Only by knowing the topography of the land at moments before the formation of the
68 gully would that question be answered with any certainty.

69 On the other hand, the width of a gully defines the upper limit of its cross section,
70 therefore conditioning the subsequent determination of the depth of that channel.
71 Furthermore, in this latter measurement (depth of the gully), another important
72 ambiguity is added, i.e. the determination of the lower limit of the cross section
73 (channel bed). This latter limit is usually located –in our belief– at the lowest point of
74 the cross section, which is questionable in beds with a highly irregular cross sectional
75 profile. Even so, nor is the difficulty inherent in measuring a gully depth usually
76 emphasized in the literature.

77 In short, the lack of any protocol or universal criterion in determining the geometry of
78 gullies would then cause a certain uncertainty at the moment of comparing between
79 each other the experimental results obtained by different researchers; for example,
80 erosion rate values.

81 In this work it is sought to make the scientific community aware of the –precisely,
82 inadvertent doubts– which are triggered when characterizing the geometry of an
83 ephemeral gully, and for this purpose some examples of real cases will be shown. Also,
84 a measurement protocol is proposed with the ultimate aim of pooling criteria in future
85 works and experimentation. Although they are proposed for ephemeral gullies, these
86 same criteria would equally apply for similar erosion channels.

87

88 **2. Uncertainties in measuring the width and depth of a gully**

89 Researchers, especially newcomers, when confronted with the measurement of gully
90 geometry, assume that the limits of the erosion channel will present themselves in the
91 field as being clearly defined, and, in fact, this is often true (see Fig. 1.1-1.3). However,
92 on many occasions this is not the case (Fig. 1.4-1.6). It is therefore possible that a clear
93 break in the slope of one of the banks (Fig. 1.6) or in both of them (Fig. 1.5) may not be
94 noticed. Another possible ambiguity –independent or added to the previous one– is that
95 which arises when both banks of the channel are uneven (Fig. 1.4, Fig. 1.6). This means
96 that determining a single height value to trace an imaginary horizontal line between
97 both banks is highly subjective. It is understood that the length of this line would be
98 defining the width of the cross section being measured.

99 In another sense, when defining the depth of a gully, the lower limit of the cross section
100 is usually well defined by the lowest point of the bed (see Fig. 1.2). However, what
101 usually happens is that the location of this limit is also controversial as can be seen in
102 the cross sections in Figures 1.1. and 1.3., where it is precisely not clear if this limit
103 would really be represented by the lower height of the bed.

104 An incorrect determination of the width and/or depth of a certain gully may cause
105 (important) errors in the determination of its volume; i.e. in the estimation of the eroded
106 soil (Fig. 2 and Fig. 3). The magnitude of this potential experimental error would be less
107 obvious, and even underestimated, if we analyze the cross sections individually (Fig. 2).
108 However, an overall review of all the sections conforming the gully being studied
109 would give a better assessment of this measurement error. Fig. 3 aims to illustrate the
110 effect that the criterion followed to determine the cross section width exerts on the
111 computed volume of a gully reach. A real gully reach was selected and three cross
112 sections were used for calculating the volume of the reach (P1, P2 and P3) (Fig. 3a), the
113 distance between cross sections being known. First, the eroded volume was calculated
114 considering a possible criterion for defining the gully cross sections width (in blue, Fig.
115 3b). Then, the eroded soil was calculated again but considering another possible
116 criterion for defining the gully cross sections widths (in red, Fig. 3b). The difference in
117 the calculated volume for both situations is remarkable, increasing by 96% from option
118 b to option c. Figure 3 is just one example illustrating: i) the great differences in
119 volumes that can be obtained in fixing the gully widths arbitrarily; ii) the error that can
120 be generated and; iii) the necessity of establishing rigorous and objective criteria and

121 protocols. The purpose of figure 3 is similar to figure 2, the latter depicting the effect of
122 the uncertainty in the determination of width in a single cross-section of a gully.

123

124 **3. Topographic definition of gully width, equivalent prismatic gully (EPG)**

125 Let's suppose that we have a detailed digital elevation model (DEM) of a gully whose
126 geometry we wish to determine (Fig. 4a). Similarly, we would also have a DEM, not
127 more than one year old, of the same area, but before the gully in question would have
128 formed. Remember that the cycle of the formation and obliteration of an ephemeral
129 gully is conditioned by the periodicity (usually one year) of the agricultural tillage
130 responsible for it. We shall call the DEM prior to the appearance of the gully $DEM_{year\ n}$,
131 whereas that of the following year –that is, with the gully now present– $DEM_{year\ n+1}$
132 (Fig. 4a).

133 Let's imagine now that, at any point x along the longitudinal axis of length L of the
134 gully, we draw a vertical plane P_x , perpendicular to that axis (Fig. 4b). If in this plane P_x
135 we subtract the $DEM_{year\ n+1}$ from the $DEM_{year\ n}$, we should obtain the eroded area or
136 cross section of the gully (Fig. 4b). Now, the imaginary line which arises from joining
137 the two points of the intersection of both DEMs would define, in turn, the width of the
138 gully in that section (P_x) (Fig. 4b). In the case of both points being uneven, a horizontal
139 projection of the line should be considered. This same operation could be repeated in a
140 multitude of other points x_i along the channel, thus obtaining the width value of each
141 new section (W_i). Finally, the average of the values W_i would define the mean
142 equivalent width of the whole gully, W_{me} . Those widths, determined thus, would
143 undoubtedly be the true transversal limit of the erosion process which caused the gully
144 in question.

145 If we now carry out the subtraction of both DEMs but on their entire surface, we
146 should obtain the volume V of the gully (Fig. 4a).

147 Also, knowing V and W_{me} , we could, in turn, determine a mean equivalent depth D_{me}
148 expressed as:

$$149 \quad D_{me} = V / (W_{me} L) \quad (1)$$

150 This depth value would be more representative of the whole gully than that resulting
151 from considering the minimum height of the bed as being the lower limit of the cross
152 section (see above).

153 Finally, the gully could be represented as a rectangular-based prism ($W_{me} D_{me}$) of a
154 length L , which we would call “equivalent prismatic gully” (EPG) (Fig. 4c and Fig. 5).
155 This sort of normalization of the complex geometry of a certain gully –by means of its
156 respective EPGs– would permit, for example, a quick visual comparison of the
157 individuals of a varied population(s) of gullies (Fig. 5). It would thus be an interesting
158 tool for incorporating into simulation models (e.g., AnnAGNPS, Gordon et al., 2007).

159 In effect, we believe that the concept of equivalent prismatic gully shows several
160 benefits and applications. Probably the principal one is that it permits the determination
161 of the most important characteristics of a complete gully (V , L , W_{me} and D_{me}), using
162 objective and repeatable criteria. Otherwise, there is the risk of assigning information
163 from specific cross sections or reaches to the whole gully. Besides, the gully properties
164 (V , L , W_{me} and D_{me}), as defined here, can be incorporated into statistical analyses or
165 similar studies in which many gullies are involved, using a common language,
166 repeatable and comparable among different researchers. Furthermore, by using the
167 concept of an equivalent prismatic gully, sets of complete gullies can easily be
168 graphically represented, which enables a quick and explanatory visual comparison.

169 The width of a gully cross section, as defined in this paper, depends on the DEMs pixel
170 size and it depends on the type and size of the studied channel. Hengl (2006) concluded
171 that, to prevent the loss of relevant information, the maximum pixel size must be the
172 average of the minimum distances between sampling points. In the same way,
173 Garbrecht and Martz (1994) fixed the pixel size to the size of the minimum
174 distinguishable object. Additionally, the new methodologies available (terrestrial or
175 aerial LIDAR, 3D photo-reconstruction, etc.), provide a very detailed information,
176 which may be more than enough, in our opinion, for the purposes of these studies.
177 However, these thresholds should be explored in future researches.

178

179 **4. Conclusions**

180 In order to progress in gully erosion research, clear criteria to define and determine the
181 key morphological characteristics of gullies and their related properties (such as
182 volumes) are needed. In this paper, a new proposal for advancing towards that goal has
183 been submitted. Thus, starting from a precise definition of the width of each gully cross
184 section, the mean equivalent gully width and depth are defined, and also the equivalent
185 prismatic gully (EPG). This approach permits the determination of the most important
186 characteristics of a complete gully (V , L , W_{me} and D_{me}), using objective criteria. Besides,
187 the gully properties defined here can be incorporated into statistical analyses using a
188 common language among different researchers. On the other hand, by using the EPG,
189 sets of complete gullies can be easily graphically represented, which allows for an
190 explanatory visual comparison. The definition of the width of each gully cross section
191 assumes that the topography of the area before the gully appearance is known. This is,
192 in fact, really infrequent, so that a new line of research arises. Anyway, we believe that
193 the proposal is a considerable advance in the applied research on gullies, because it
194 allows one to standardize the definition and determination of the most important
195 characteristics of these erosion forms.

196

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200

201 **References**

202

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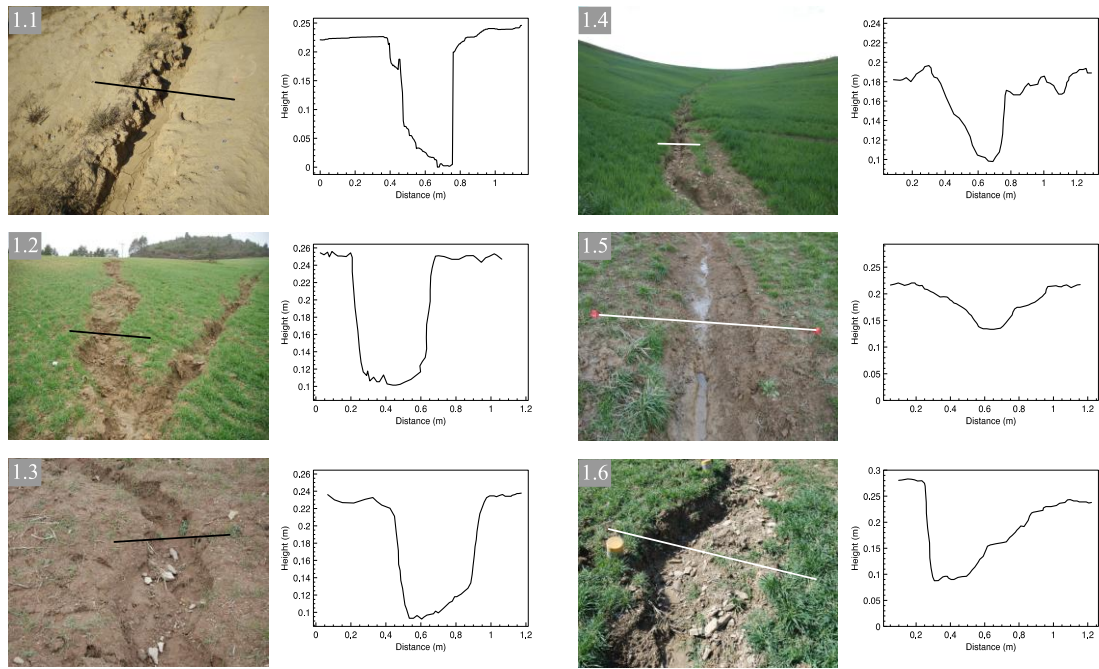
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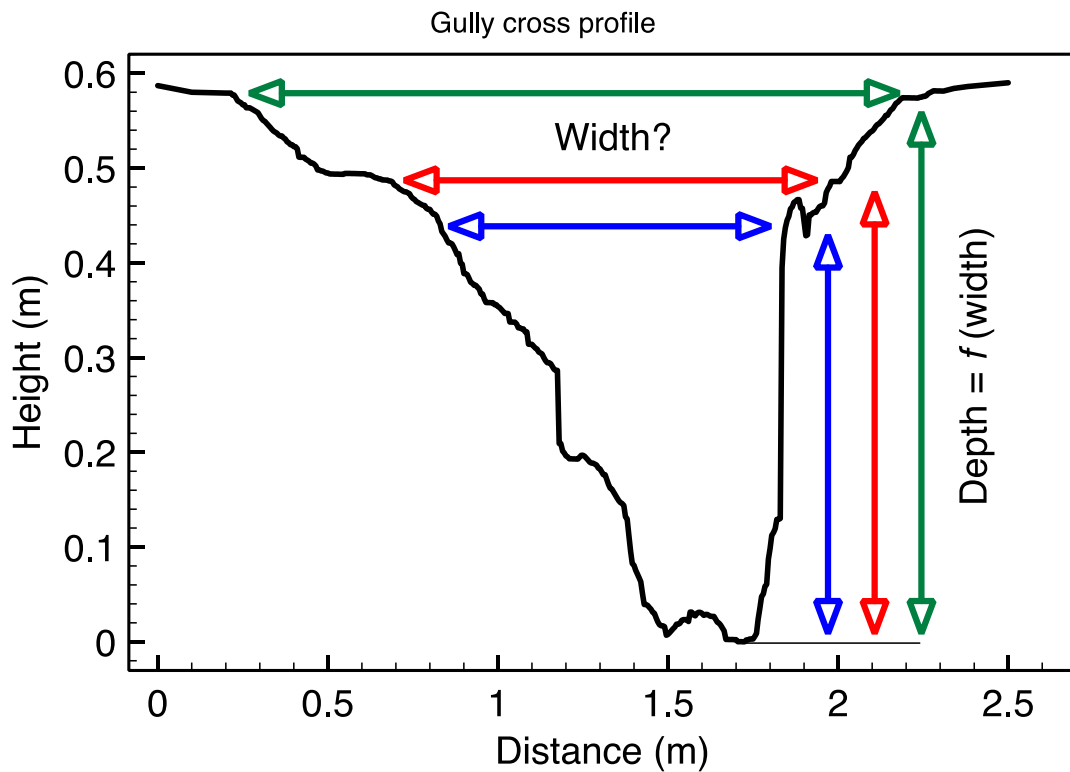
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244 **Figures**



245

246 Figure 1. Examples of cross-sections of typical ephemeral gullies (Navarre, Spain).

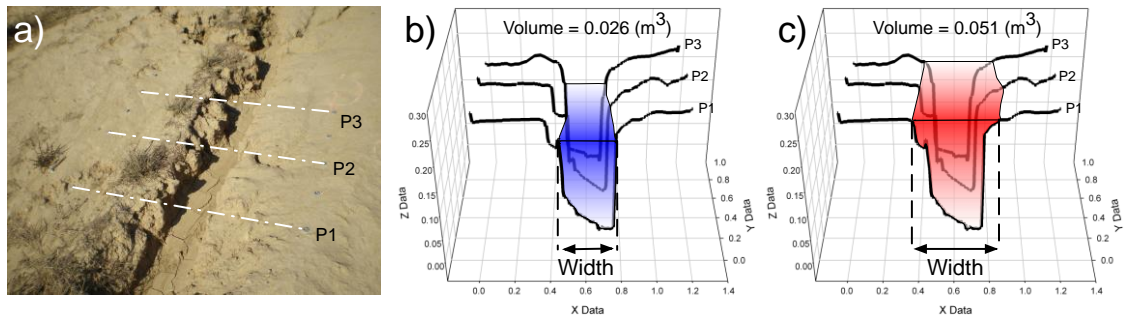


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248 Figure 2. Uncertainty in the determination of a width in a cross-section of a gully (real
249 example).

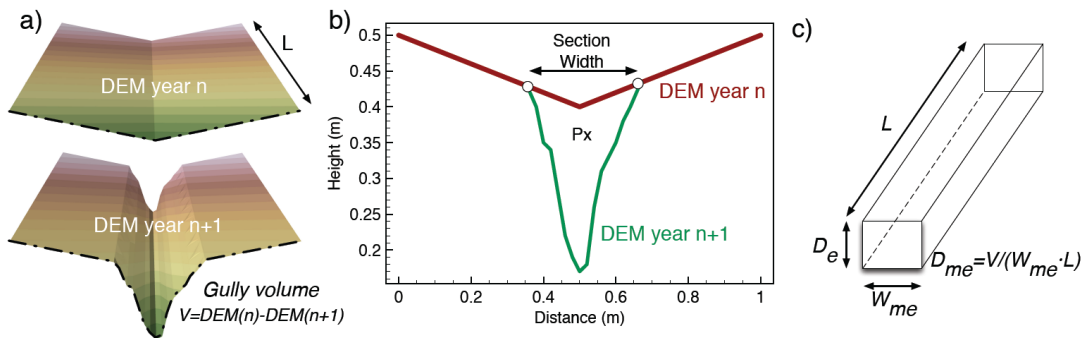
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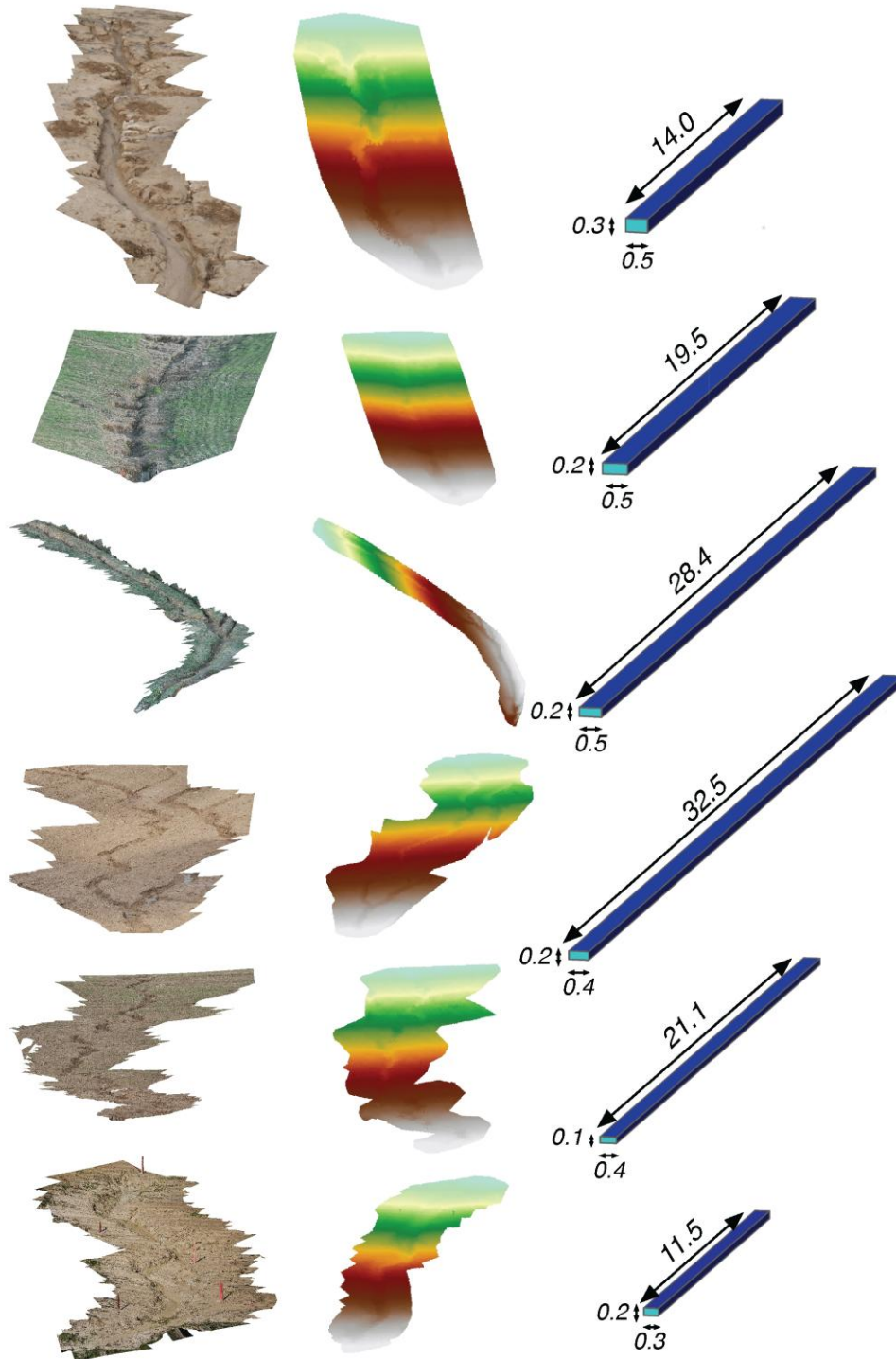
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253 Figure 3. Illustration of the effect that the criterion followed to determine the cross
254 section width exerts on the computed volume of a gully reach. a) Selected gully reach
255 and location of the three cross sections used for calculating the volume of the reach (*P1*,
256 *P2* and *P3*); the distance between cross sections is known. b) Calculated eroded volume
257 (in blue) when considering a possible criterion for defining the gully cross sections
258 widths. c) Calculated eroded volume (in red) when considering another possible
259 criterion for defining the gully cross sections widths.



260

261 Figure 4. a) Sketch of two separated digital elevation models of a fictitious plot before
262 ($DEM_{year\ n}$) and after ($DEM_{year\ n+1}$) a gully has been formed in the plot thalweg; b)
263 sketch cross section area depicted at any point x along the longitudinal axis of the gully;
264 c) equivalent prismatic gully (EPG). See section 3 for details.



265

266 Figure 5. a) Pictures of ephemeral gullies of different shapes (Navarre, Spain); b)
 267 Digital elevation model ($DEM_{year\ n+1}$, see Figure 4) of each gully; c) Equivalent prism of
 268 the gullies (since there was not a DEM available prior to the gully formation ($DEM_{year\ n}$,
 269 see Figure 4) the width was arbitrarily defined from abrupt changes at both gully banks
 270 (see text for more explanation). It should be made clear that the geometry of the
 271 equivalent prisms could have (dramatically) changed if we had also counted with the
 272 corresponding $DEM_{year\ n}$. (Lengths in m)